

Institut für Diskrete Mathematik

**Vortrag im Seminar für Kombinatorik und Optimierung**

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**On the number of arithmetic progressions in sparse random sets**

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We study arithmetic progressions  $\{a, a + b, a + 2b, \dots, a + (\ell - 1)b\}$ , with  $\ell \geq 3$ , in random subsets of the initial segment of natural numbers  $[n] := \{1, 2, \dots, n\}$ . Given  $p \in [0, 1]$  we denote by  $[n]_p$  the random subset of  $[n]$  which includes every number with probability  $p$ , independently of one another. The focus lies on sparse random subsets, i.e. when  $p = p(n) = o(1)$  with respect to  $n \rightarrow \infty$ .

Let  $X_\ell$  denote the number of distinct arithmetic progressions of length  $\ell$  which are contained in  $[n]_p$ . We determine the limiting distribution for  $X_\ell$  not only for fixed  $\ell \geq 3$  but also when  $\ell = \ell(n) \rightarrow \infty$  sufficiently slowly. Moreover, we prove a central limit theorem for the joint distribution of the pair  $(X_\ell, X_{\ell'})$  for a wide range of  $p$ . Our proofs are based on the method of moments and combinatorial arguments, such as an algorithmic enumeration of collections of arithmetic progressions.

These results are joint work with Y. Barhoumi-Andréani and H. Liu (Warwick).

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