

## Deformations of complexity-one rational $T$ -varieties

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Let  $X_0$  be any rational normal variety with an effective action by some torus  $T$  of codimension one. In [2], R. Vollmert and I developed a combinatorial construction with which one can describe homogeneous deformations  $\pi : X \rightarrow S$  of such  $X_0$ . If  $X_0$  is smooth, complete, and toric, these deformations span the space of infinitesimal deformations. In fact, in this case,  $H^1(X_0, \mathcal{T}_{X_0})$  can be easily read off from the fan corresponding to  $X_0$ , see [1].

It turns out that if  $\pi$  is locally trivial, for any point  $s \in S$  there exists a natural map  $\pi_s^0 : \text{T-CaDiv}(X_s) \rightarrow \text{T-CaDiv}(X_0)$ , where  $\text{T-CaDiv}$  denotes the group of  $T$ -invariant Cartier divisors; this map is one of the subjects of study in [3]. Some of the main results can be summarized as follows:

**THEOREM.** *If  $X_0$  is complete, then the map of divisors  $\pi_s^0$  induces an isomorphism of Picard groups  $\bar{\pi}_s^0 : \text{Pic}(X_s) \rightarrow \text{Pic}(X_0)$  such that for every  $\mathcal{L} \in \text{Pic}(X_s)$ ,*

1.  $\chi(\bar{\pi}_s^0(\mathcal{L})) = \chi(\mathcal{L})$ ;
2.  $h^i(\bar{\pi}_s^0(\mathcal{L})) \geq h^i(\mathcal{L})$  for all  $i \geq 0$ .

In this talk, I will outline these recent results in a form requiring no prior knowledge of toric geometry. In a following talk, A. Hochenegger will apply some of these results to the study of exceptional sequences of lines bundles on rational  $\mathbb{C}^*$ -surfaces.

- [1] N. ILTEN: *Deformations of Smooth Toric Surfaces*. arXiv:0902.0529v3 [math.AG], 2009.
- [2] N. ILTEN AND R. VOLLMERT: *Deformations of Rational  $T$ -Varieties*. arXiv:0902.0529v3 [math.AG], 2009.
- [3] A. HOCHENEGGER AND N. ILTEN: *Families of Divisors on  $T$ -Varieties and Exceptional Sequences on  $\mathbb{C}^*$ -Surfaces*. arXiv:0906.4292v1 [math.AG], 2009.