

Institut für Optimierung und Diskrete Mathematik

## Vortrag im Seminar Diskrete Mathematik und Optimierung

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Seminarraum C208, Steyrergasse 30, 2. Stock

# Algorithms and automata for the Tower of Hanoi<sup>1</sup>

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Mathematical solitaire games like the Chinese Rings and the Tower of Hanoi can be modelled by state graphs, leading to the two-parameter classes of Sierpiński graphs  $S_p^n$  and Hanoi graphs  $H_p^n$ . Shortest path algorithms can be based on automata in the Sierpiński case, so that the metric properties of  $S_p^n$  (and  $H_3^n \cong S_3^n$ ) are now completely understood. For Hanoi graphs with  $p > 3$ , however, the notorious Frame-Stewart Conjecture (1941) is still undecided and unexpected behavior of eccentricities like Korf's Phenomenon (2004) remains unexplained. Whereas  $\text{diam}(S_p^n) = 2^n - 1$  for all  $p \geq 2$ , the diameter of  $H_p^n$  is known only for small values of the parameters by computer experiments.

### References.

- [1] Hinz, A.M., Klavžar, S., Milutinović, U., Petr, C., The Tower of Hanoi—Myths and Maths, Springer, Basel, 2013.
- [2] Hinz, A.M., Holz auf der Heide, C., An efficient algorithm to determine all shortest paths in Sierpiński graphs, *Discrete Appl. Math.* 177(2014), 111–120.

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