

## Institut für Diskrete Mathematik

## **Combinatorics Seminar**

Friday 19th April 12:30

Online meeting (Webex)

## The structure and density of (strongly) k-product-free sets in the free semigroup.

## FREDERICK ILLINGWORTH

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The free semigroup  $\mathcal{F}$  over a finite alphabet  $\mathcal{A}$  is the set of all finite words with letters in  $\mathcal{A}$  equipped with the operation of concatenation. A subset S of  $\mathcal{F}$  is k-product-free if no k words in S concatenate to another word in S. How dense can a k-product-free subset of  $\mathcal{F}$  be? What is the structure of the densest k-product-free subsets?

Leader, Letzter, Narayanan, and Walters proved that 2-product-fee subsets of the free semigroup have density at most 1/2 and asked for the structure of the densest sets. In this talk I will discuss the answer to their question as well as the answer (both density and structure) for general k. This generalises results of Luczak and Schoen for sum-free sets in the integers although the methods used are quite different.

This is joint work with Lukas Michel and Alex Scott.

Meeting link:

 $https://tugraz.webex.com/tugraz/j.php?MTID {=} m8500c46344212abf0fa37925da5ef9bf$ 

Joshua Erde, Mihyun Kang