The operator div A grad for sign-indefinite A

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Differential expressions of the type $\operatorname{div} A(\cdot)$ grad with sign-indefinite coefficient matrix $A(\cdot)$ arise in the modelling of metamaterials with negative refraction index.

Using the representation theory for indefinite quadratic forms, we prove, that these differential expressions define self-adjoint operators on bounded domains.

The spectral asymptotics and solvability of boundary value problems for this operator is discussed as well.

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