Large time behaviour of heat kernels and admissible potentials

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Let T be a positivity improving selfadjoint C_0 -semigroup on $L_2(\Omega, \mu)$ with generator -H. The following two questions are going to be addressed in the talk:

- Assuming the semigroup operators T(t) have integral kernels p_t , what is the long time behaviour of $p_t(x, y)$, given $x, y \in \Omega$?
- For a measurable potential $V \colon \Omega \to [0, \infty)$, when does the initial value problem

$$u'(t) + Hu(t) = Vu(t) \quad (t > 0), \qquad u(0) = u_0$$

have a positive exponentially bounded solution, given a positive initial value $u_0 > 0$?

The talk is based on joint work with M. Keller, D. Lenz and R. Wojciechowski.